Indium antimonide—Constraints on practicality as a magneto-optical platform for topological surface plasmon polaritons

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ABSTRACT

Magnetic-field-biased indium antimonide (InSb) is one of the most widely discussed materials for supporting nonreciprocal surface plasmon polaritons (SPPs), which have recently been shown to be topological. In this work, we provide a critical assessment of InSb as a magneto-optical SPP platform and show that it is only viable under a narrow set of conditions.

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I. INTRODUCTION

Continuous media with broken time-reversal symmetry, such as a magnetized semiconductor, have recently been shown to be topologically nontrivial.¹⁻⁴ Topological surface waves have unique optical properties, namely, one-way propagation (immunity to backscattering), and since they exist in the bulk bandgap, upon encountering discontinuities, they do not diffract into the bulk.^{5,6} Topological effects in photonic systems are promising in the realization of devices such as optical isolators and circulators.

Theoretical/simulation studies of nonreciprocal SPPs, including topological SPPs, often cite InSb as an example of a material providing the necessary gyrotropic permittivity tensor.8-17 However, here, we show that, while SPPs with reasonable propagation characteristics

can be obtained, there exist severe constraints that limit performance. In particular, we find that for InSb to serve as a viable SPP platform under modest bias field strengths, one needs to use undoped materials and low, but not too-low, temperatures to obtain sufficiently high mobility and a reasonably sized bulk bandgap.

In the following, there is a brief review on topological SPP properties in a dissipation-less system in the Voigt configuration in which the propagation vector is perpendicular to the in-plane magnetic bias, and there are topological SPPs crossing the bulk bandgaps of the gyrotropic plasma medium. Next, using time-domain spectroscopy (THz-TDS), the measured reflection from a magnetized InSb crystal is considered. Using the measured parameters at different temperatures, the properties of topological SPPs in a realistic plasma material are examined. It is shown that temperature

plays an important role in optimizing the SPP propagation properties. Last, with the help of a symmetric grating launcher, the SPPs are observed at the interface of gold/InSb at various temperatures using a far-field measurement. The measured SPP resonance frequencies are consistent with the values theoretically estimated.

II. ELECTROMAGNETIC MODEL AND RESULTS

A. Material model and bulk modes

Consider a half-space plasma medium (InSb) with unit normal vector \hat{z} , biased by an in-plane external magnetic field $\mathbf{B}_0 = \widehat{\mathbf{y}} B_0$. The gyrotropic InSb can be characterized by a simplified Drude model with a dielectric tensor in the form $\mathbf{\bar{e}}_r = \varepsilon_r \mathbf{\bar{I}}_t + i\varepsilon_g (\widehat{\mathbf{y}} \times \mathbf{\bar{I}}) + \varepsilon_a \widehat{\mathbf{y}} \widehat{\mathbf{y}}$ (assuming the time harmonic variation $e^{-i\omega t}$), where

$$\varepsilon_{t} = \varepsilon_{\infty} - \frac{\omega_{p}^{2} (1 + i\Gamma/\omega)}{(\omega + i\Gamma)^{2} - \omega_{c}^{2}}, \quad \varepsilon_{a} = \varepsilon_{\infty} - \frac{\omega_{p}^{2}}{\omega(\omega + i\Gamma)},$$

$$\varepsilon_{g} = \frac{\omega_{c} \omega_{p}^{2}}{\omega[\omega_{c}^{2} - (\omega + i\Gamma)^{2}]},$$
(1)

and where ε_{∞} is the background permittivity (high-frequency dielectric constant). The plasma frequency is $\omega_p = \sqrt{n_e q_e^2/(m^*\varepsilon_0)}$, $\omega_c = -q_e B_0/m^*$ is the cyclotron frequency, and $\Gamma = -q_e/\mu m^*$ is the collision frequency. Also, n_e is the free electron density, $q_e = -e$ is the electron charge, ε_0 is the free-space permittivity, $m^* = m_{\rm eff} \ m_0$ is the effective electron mass, m_0 is the vacuum electron mass, and μ is the mobility. In the absence of a magnetic bias, the gyrotropic plasma turns to a dispersive isotropic medium having permittivity ε_a . Here, we ignore the phonon contribution in the material model, which is an accurate assumption at frequencies below the optical phonon resonances (and at low temperatures). There are also contributions from heavy and light hole bands, ¹⁹ but

both were found to be negligible, the former because of the large mass and the latter due to a small carrier density even at room temperature. The plasma frequency ω_D sets the frequency scale for the occurrence of bandgaps, and we need a sufficient magnetic bias so that the cyclotron frequency ω_c is not too small compared to ω_p in order to achieve a usual amount of nonreciprocity. The characteristics of the bulk modes in a gyrotropic medium depend on the direction of propagation with respect to the external magnetic bias. In the well-known Voigt configuration, the bulk modes are propagating perpendicular to the magnetic bias. In this case, the bulk waves can be decoupled into a TE (with the electric field along the magnetic bias) and a TM (with the electric field in a plane perpendicular to the bias) wave described by $k_{\rm TE}^2 = \varepsilon_{\rm a} k_0^2$ and $k_{\rm TM}^2 = \varepsilon_{\rm eff} k_0^2$, respectively, where $\varepsilon_{\rm eff} = (\varepsilon_t^2 - \varepsilon_g^2)/\varepsilon_t$ and k_0 is the free-space wave number. Figure 1(a) (black lines) shows the dispersion diagram of TM bulk modes propagating in dissipation-less InSb. There are two magnetic-field dependent bandgaps. Each TM band is characterized by a non-zero integer Chern number C_n , an intrinsic property of the bulk band structure, so that Chern numbers sum to zero, as expected.²⁰ The gap Chern number, that is, the sum of the Chern numbers below the gap, is non-zero, indicating the number of topologically protected surface modes crossing the bandgaps. The TE mode, with $C_n = 0$, is topologically trivial and will not be discussed further. Here, in the material model, non-locality is ignored except to provide a momentum cutoff.² The effect of non-locality is evident only for very large wavenumbers²¹ in which case the backward waves vanish for realistic levels of loss.22

B. Surface plasmon polaritons

0.5

-0.5

Despite the non-reciprocal nature of the medium itself, in the Voigt configuration, the bulk dispersion behavior is reciprocal, although an interface will break this reciprocity. The TM-SPP

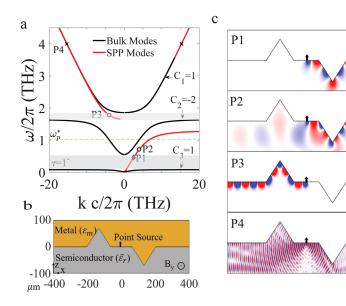


FIG. 1. Bulk modes and surface plasmons for a metal-InSb (idealized) interface. (a) Bulk and SPP dispersion for dissipation-less InSb characterized by (1) with parameters $n_e=3\times 10^{21}\,\mathrm{m}^{-3}, \quad m^*=0.015\,\mathrm{m}_0, \quad \varepsilon_\infty=15.68,$ and mobility $\mu=\infty \quad [\omega_p^*=\omega_p/\sqrt{\varepsilon_\infty}=2\pi(1.014\,\mathrm{THz})].$ The carrier densities and other numerical values have been obtained from fitting (1) to measurements. 20 The in-plane magnetic field is $B=0.7\,\mathrm{T} \ [\omega_c=1.28\omega_p^*=2\pi(1.3\,\mathrm{THz})],$ and the metal permittivity is $\varepsilon_m=-10^4.$ The gray regions are the magnetic-field dependent bandgaps. (b) The geometrical schematic of the structure under study. SPPs are excited by a dipole source located at the metal–InSb interface. (c) The electric field distribution (E_z) of SPPs at different frequencies P1–P4, 0.5, 0.7, 1.76, and 4 THz, respectively, marked in (a). Points P1 and P3 are points on the SPP dispersion where the SPPs are topologically protected.

dispersion equation is 1,23

$$\frac{\gamma_{zm}}{\varepsilon_m} + \frac{\gamma_z}{\varepsilon_{\text{eff}}} = \frac{\varepsilon_g k_x}{\varepsilon_t \varepsilon_{\text{eff}}},\tag{2}$$

where $\gamma_z = \sqrt{k_x^2 - k_0^2 \varepsilon_{\rm eff}}$, $\gamma_{zm} = \sqrt{k_x^2 - k_0^2 \varepsilon_m}$, and ε_m is the effective permittivity of the top (metal) layer. The SPP is propagating on the x-y plane (interface of two media) with the propagation constant k_x . If isotropic materials form the interface, for an SPP to propagate, the two permittivities must have opposite signs. In the gyrotropic plasma-isotropic metal case, it can be shown analytically that in the bandgaps, where $\varepsilon_{\rm eff} < 0$, for an SPP to exist, we need $\varepsilon_t > 0$. Outside of the bandgaps, it can be seen numerically that no SPP exists when $\varepsilon_t < 0$.

Figure 1(a) shows the dispersion of the SPP at the interface of a dissipation-less gyrotropic semiconductor and an opaque medium (red lines), with the interface geometry depicted in Fig. 1(b). Figure 1(c) shows the electric field profile of SPP propagation at different points on the dispersion curve, P1-P4, shown in Fig. 1(a), obtained from a full wave simulation using COMSOL assuming a dipole source. As discussed above, SPPs crossing the bandgaps, for example, at frequency points P1 and P3, are topologically protected surface waves, meaning that they are unidirectional and propagate along the surface without reflection. In the frequency range between the two bandgaps, although the dispersion is strongly nonreciprocal, upon reflection, surface waves can couple into the bulk modes; see, e.g., point P2. At higher frequencies, for example, at point P4, SPPs are bi-directional; the right- and left-going SPPs have approximately the same momentum, $\omega(k) = \omega(-k)$. Partial reflection of the wave occurs since at this frequency, the material itself allows propagation in both directions.

C. Realistic InSb model

The previous discussion was for lossless materials. In the following, the properties of bulk and topological SPPs for a realistic InSb model are examined. We consider that for SPP applications, we require, or it is at least very desirable, that (1) $L_{\rm SPP}/\lambda_{\rm SPP}\gg 1$, where the SPP propagation length is $L_{\rm SPP}=1/(2{\rm Im}(k_{\rm SPP}))$ and the SPP wavelength is $\lambda_{\rm SPP}=2\pi/{\rm Re}(k_{\rm SPP})$, (2) SPPs that are nonreciprocal so that they are backscattering-immune, and (3) SPPs exist in the bulk bandgaps so that they will not diffract into the bulk upon encountering a discontinuity. To meet these criteria, the requirements on the material properties are very stringent.

In the experiment, we use an InSb crystal from the manufacturer MTI Corporation²⁴ having dimensions $10 \times 10 \times 0.5 \, \mathrm{mm}^3$, undoped, with one side polished. In Ref. 26, we have extracted the carrier density, mobility, and effective mass of InSb at various temperatures from 5 K to 300 K and under external bias fields up to 0.7 T, determined by far-field time-domain terahertz spectroscopy (THz-TDS) in the range of 0.5–3 THz. Four material samples were tested, and the results below represent values from one of the samples (two others were similar, and one showed poorer performance). For the metal, we assume that $\varepsilon_m = -800 + i550.^{25}$ If the metal is less lossy, longer propagation lengths will be obtained. Also, note that L_{SPP} was not directly measured but was calculated based on the measured material parameters.

Figures 2(a), 2(c), and 2(e) show the reflectance spectra, $\tilde{R} = r(B)/r(0)$, of an air/InSb sample measured at different temperatures for B = 0.7 T. The material parameters can be obtained using the Drude model and the analytical reflection coefficient in the Voigt configuration defined as

$$R_{TM} = \frac{\sqrt{\varepsilon_{\text{eff}}} - \sqrt{\varepsilon_d}}{\sqrt{\varepsilon_{\text{eff}}} + \sqrt{\varepsilon_d}},\tag{3}$$

where ε_d is the permittivity of the isotropic material (here, $\varepsilon_d=1$) and $r=|R_{TM}|^2$. As shown in Figs. 2(a), 2(c), and 2(e), the carrier concentration decreases as the temperature decreases, resulting in shifting the reduced edge plasma frequency, $\omega_p^*=\omega_p/\sqrt{\varepsilon_\infty}$, toward lower frequencies. In the bandgap, the transparency of the biased crystal increases, causing the second peak in the reflectance spectrum, which is a function of cyclotron frequency, plasma frequency, and magnetic bias. As the temperature decreases down to 50 K, the mobility increases as expected since the scattering rate increases with the temperature.

Based on the measured material parameters, the SPP dispersion diagram and the propagation length of the SPP excited at the interface of a gold/InSb interface at each temperature are shown in Figs. 2(b), 2(d), and 2(f). At lower temperatures, the propagation length is larger due to the higher mobility, although the bandgaps become very narrow.

Figure 3(a) shows the bulk and SPP dispersion for InSb at 230 K. Loss leads to modified bulk plasmon dispersions in which case there no longer exists a true bandgap [comparing the solid black lines in Fig. 3(a) with the dotted black lines, which indicate the dissipation-less case from Fig. 1(a)]. However, there are still distinguishable regions of dispersion. The field profile of the SPPs at two dispersion points P1 and P2 [Fig. 3(a)] is shown in Fig. 3(b). In a dissipative system, nonreciprocal (unidirectional) SPPs are still immune to backscattering upon encountering a discontinuity. Figure 3(c) shows the propagation length of SPPs supported by InSb at three different temperatures. At high temperature, the mobility is low ($\mu = 5.2 \,\mathrm{m^2/Vs}$) so that the propagation length of the one-way SPP (at frequencies below the dashed line, where SPPs are nonreciprocal) is a small fraction of the SPP wavelength [Fig. 3(c), black curve]. By reducing the temperature, the bandgap range decreases, but the mobility increases, resulting in longer propagation lengths as shown in Fig. 3(c), blue curve. In each case, only to the left of the dashed vertical lines the SPP is nonreciprocal. Moreover, only along the dashed sections is the SPP within the bandgaps.

In Table I, the values for the bandgap frequency range and the propagation length of the nonreciprocal SPPs at different frequencies, in and between the two bandgaps, and at various temperatures are listed for $B=0.7\,\mathrm{T}$. As shown, there is a trade-off between the propagation length and the size of the bandgap—as the temperature is lowered, the bandgap can become quite narrow and impractical. Therefore, the temperature needs to be carefully chosen, low enough to yield sufficient SPP propagation lengths, yet not too low so that the bandgap is wide-enough to work within. Furthermore, unless the magnetic bias is adjusted appropriately, the SPP will not exist within the bandgap.

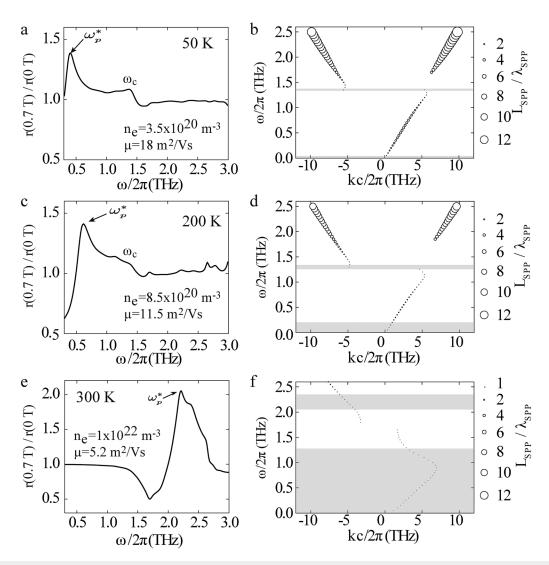


FIG. 2. (a), (c), and (e) Experimentally measured reflectance spectra of the InSb sample at different temperatures. The values for n_e and μ in each panel are the extracted InSb parameters by fitting measurement data to the Drude model. (b), (d), and (f) The SPP dispersion diagrams and the SPP propagation length (indicated by the size of the circles). Shaded regions indicate the bandgaps.

Given that one may consider operation within the bandgap as most desirable, for this bias, only for the lowest temperature is $L_{\rm SPP}/\lambda_{\rm SPP}\approx 1$, although longer propagation lengths are found between the two bandgaps. Similar to Table I, Fig. 3(d) shows a density plot of SPP propagation length $\Lambda_{\rm SPP}=L_{\rm SPP}/\lambda_{\rm SPP}$ vs frequency and temperature. The temperature-bandgap width trade-off is prominent, as are the relatively short values of the non-reciprocal SPP propagation length except between the bandgaps. Table II provides a comparison of SPP properties between undoped, N-doped, and P-doped samples at $T=77\,\rm K$. For the undoped case, material parameter values were taken from measurements, ²⁶ whereas for the doped cases, we used parameter values from the manufacturer's website. ²⁴ The P-doped case has very low mobility and poor SPP

properties and will not be discussed further. The undoped case discussed above provides good SPP propagation below 2 THz and $T \lessapprox 200$ K. Because of the large carrier density in the N-doped case, the plasma frequency, and, hence, the upper bandgap, occurs at higher frequency than for the undoped case, around 10 THz for B=0.7 T. However, for this strength bias, ω_c/ω_p is small, and poor SPP propagation is obtained. In order to obtain comparable SPP performance for the N-doped material, one would need B=15 T, which is difficult to obtain, at which point the higher bandgap occurs near 30 THz (here, we assume that the mobility is the same as the low-THz values).

In summary, one may conclude that for working at low THz (\lesssim 2 THz) and moderate bias strength (\lesssim 1 T), the undoped material

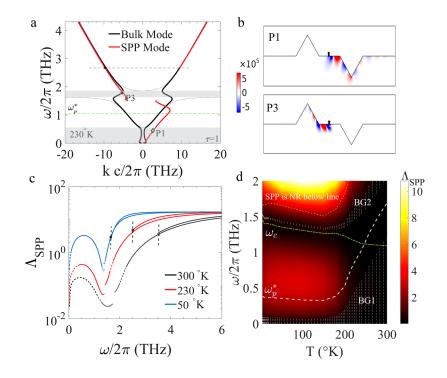


FIG. 3. Bulk modes and nonreciprocal InSb-metal interface SPPs for a realistic InSb model with finite dissipation: (a) and (b) bulk and SPP dispersion diagrams using InSb material parameters at $T=230\,\mathrm{K}$, which are $n_{\rm e} = 3 \times 10^{21} \, {\rm m}^{-3}, \quad \mu = 9 \, {\rm m}^2/{\rm Vs}, \quad m^* = 0.015 \, {\rm m}_0,$ $arepsilon_{\infty}=$ 15.68, extracted from measurement, 26 and B = 0.7 T, $\varepsilon_m = -800 + i550$. Solid lines correspond to finite dissipation and dotted lines correspond to the infinite mobility cases. Below the dashed horizontal line, the SPP is nonreciprocal (NR) and sometimes unidirectional. (b) The electric field distribution of the unidirectional SPP, at two resonance frequencies P1 and P2, excited by a point source located at the interface for the finite-mobility case. (c) The SPP propagation length ($L_{\rm SPP}$) in a dissipative system at three different temperatures, where Λ_{SPP} = $L_{\text{SPP}}/\lambda_{\text{SPP}}$. To the left of the dashed vertical lines, the SPP is nonreciprocal. The dashed sections indicate that the SPP is within the bandgaps. (d) Density plot of normalized SPP propagation length, Λ_{SPP} , vs frequency and temperature. Shaded regions indicate the bandgaps.

TABLE I. SPP propagation length and the bandgap width in frequency at various temperatures. BG₁ (which starts at 0 THz; the provided value is for the top of the bandgap) and BG₂ are the lower and upper bandgaps, respectively. BTWN-BGs indicate at the midpoint between the two bandgaps (in the bulk passband), $\varepsilon_m = -800 + i550$, $E_m = -800 + i550$, and $E_m = -800 + i550$, and $E_m = -800 + i550$, $E_m = -800 + i550$, and $E_m = -800 + i550$.

Temperature (K)	300	250	200	150	100	50
BG ₁ (THz)	1.23	0.72	0.19	0.08	0.08	0.08
BG ₂ (THz)	2.01-2.32	1.60 - 1.84	1.33-1.41	1.30-1.34	1.35-1.38	1.39-1.43-
Λ in-BG ₁	0.17	0.30	0.76	0.91	1.03	1.00
Λ BTWN-BGs	0.03	0.25	1.20	2.90	3.30	3.30
Λ in-BG ₂	0.46	0.48	0.50	0.75	0.66	0.61

TABLE II. Comparison of plasmon propagation properties in the undoped, N-doped, and P-doped crystals at T = 77 K, considering $m^* = 0.015 \,\mathrm{m}_0$, $\varepsilon_\infty = 15.7$, and $\varepsilon_m = -800 + i550$. $\Lambda = L_{\mathrm{SPP}}/\lambda_{\mathrm{SPP}}$ Dashes indicate that no SPP exists. BG₁ starts at 0 THz; the provided value is for the top of the bandgap.

T = 77 K	Undoped	N-doped 350		P-doped 35
$n_e \times 10^{21} (\text{m}^{-3})$	0.32			
μ (m ² /Vs)	17	4.5		0.2
$\omega_p^*/2\pi (\mathrm{THz})$	0.33	10.9	10.9	3.4
B (T)	0.7	0.7	15	0.7
ω_c/ω_p^*	3.9	0.12	2.5	0.37
Γ/ω_p	0.08	0.01	0.01	0.7
BG ₁ (THz)	0.08	10.3	3.70	2.9
BG ₂ (THz)	1.35-1.38	11.0-11.6	30.0-31.7	3.7-4.2
Λ in-BG1	1.0	0.02	1.6	0.2
Λ BTWN-BGs	3.3		3.3	
Λ in-BG2	0.65	0.5	1.1	•••

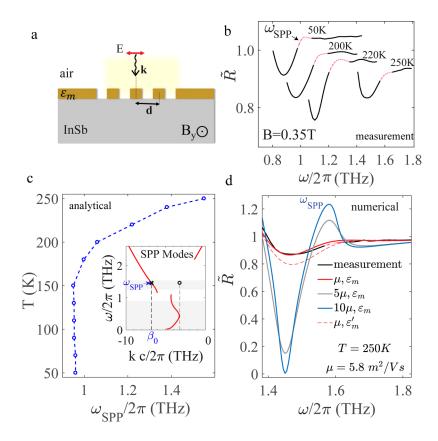


FIG. 4. The far-field measurement of the unidirectional SPP at various temperatures. (a) The schematic geometry of the structure under test. The SPP is excited using a symmetric metal grating under a normally incident plane wave. The period of grating is $d=84\,\mu\mathrm{m}$, and the metal thickness is $t = 0.5 \,\mu\text{m}$. (b) The reflection spectrum of the pattern InSb sample is measured at various temperatures. \tilde{R} is defined as the ratio of r(B)/r(0), where r(B) and r(0) are the reflectance of the biased/unbiased pattern sample, respectively. The red peaks are observed unidirectional SPP resonances. (c) The analytically estimated SPP resonance frequencies at different temperatures, obtained using the SPP dispersion diagram and the effective momentum $eta_0=2\pi/d$ due to the symmetric grating as illustrated in the inset plot. (d) The reflection spectrum of the pattern InSb results from a COMSOL simulation. The InSb crystal is characterized by $n_e=4.5\times 10^{21}\,\mathrm{m}^{-3},~m^*=0.0175\,\mathrm{m}_0,~\varepsilon_\infty=15.68,$ and different mobility values. $\varepsilon_m = -800 + i550$, $\varepsilon_m' = (-2.3 + i8.6) \times 10^5$, and B = 0.35 T.

is the only viable option. Room temperature operation is not feasible. For the N-doped material, aside from $B=15\,\mathrm{T}$, below $\lesssim 5\,\mathrm{T}$, there is no SPP between the two bandgaps, but for bias levels such as B=5,7.5, and 12 T, the maximum $L_{\mathrm{SPP}}/\lambda_{\mathrm{SPP}}$ is 0.4, 1.1, and 2.3, respectively. If an n-doped InSb crystal with a lower level of doping is used, a weaker magnetic bias would be required (still, several T) to obtain SPPs with reasonable propagation lengths. However, the bias and the bandgap frequency range are still very much higher than for the undoped case.

It is worth noting that properties of the metal layer also impact performance. For example, using parameters of the undoped sample in Table II, if the metal permittivity were $\varepsilon_m' = (-2.3 + i8.6) \times 10^5$ obtained using a standard Drude model, the maximum propagation length of the SPP between two bandgaps is $7.4\lambda_{SPP}$, more than twice the value reported in Table II. Metal deposition quality, surface roughness, etc., will also play an important role, which are not the subject of this work. However, for some applications such as switches and nonlinear devices, a very long SPP propagation length is not required.

In order to excite SPPs in the experiment, a symmetric metal grating is used as the SPP launcher. Figure 4(a) shows the geometry of the structure, an InSb sample covered with a grating under a normally incident plane wave. The electric field polarization is perpendicular to the grating strips as well as the magnetic bias. Figure 4(b) shows the measured reflectance spectra \tilde{R} of the

magnetized pattern InSb sample at various temperatures. The red peaks indicate the SPP resonances of the biased sample. By applying B = 0.35 T, the SPP resonance frequencies are within or above the upper bandgap, depending on the frequency. The period of the grating is $d = 84 \,\mu\text{m}$ with the filling factor 1/2, providing the effective momentum $\beta_0 = 2\pi/d$ for the system under a normally incident plane wave. Using the SPP dispersion diagram, the SPP resonance frequency can be obtained at different temperatures as shown in Fig. 4(c). The measured resonance frequencies are consistent with the values theoretically estimated. Figure 4(d) shows the reflection spectrum of the pattern InSb obtained using a COMSOL simulation. As an example, for $T = 250 \,\mathrm{K}$ and considering a realistic value of mobility ($\mu = 5.8 \,\mathrm{m}^2/\mathrm{Vs}$) as shown, the numerical result is well-matched with the measurement result. The reflectance corresponding to larger mobility has also been shown in Fig. 4(d). If the mobility were higher, the SPP resonance becomes stronger; the red resonance peaks in Fig. 4(b) become larger.

Finally, in Fig. 4(d), simulation results for reflectance are shown for a metal grating having permittivity $\varepsilon_m' = (-2.3 + i8.6) \times 10^5$, the standard Drude model (red-dashed curve). It can be seen that the THz-measured value²⁵ used in this work, $\varepsilon_m = -800 + i550$, provides a better agreement with the measurement than the higher-permittivity model, leading to confidence in this lower value. We note that the two different metal permittivity values do not significantly change the resonance frequencies shown in Fig. 4(c).

III. CONCLUSION

In this work, we studied the low-THz characteristics of the SPPs on a metal–InSb interface with a realistic InSb model. SPPs in the bulk bandgaps are topological, and to design wideband devices based on topological SPPs, the propagation length and the bandgap size are two important factors. For very low temperatures, InSb is not a suitable platform for topological SPPs due to an extremely narrow bandgap, whereas for higher temperatures (say, above 250 K), the propagation length is not long enough due to low mobility. At temperatures between 150 K and 220 K, moderate bandgap width and $L_{\rm SPP}/\lambda_{\rm SPP} \gtrapprox 1$ are obtainable using undoped InSb.

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DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

REFERENCES

- ¹A. R. Davoyan and N. Engheta, "Theory of wave propagation in magnetized near-zero-epsilon metamaterials: Evidence for one-way photonic states and magnetically switched transparency and opacity," Phys. Rev. Lett. 111, 257401 (2013).
- ²M. G. Silveirinha, "Chern invariants for continuous media," Phys. Rev. B **92**, 125153 (2015).
- ³M. G. Silveirinha, "Bulk-edge correspondence for topological photonic continua," Phys. Rev. B **94**, 205105 (2016).
- ⁴S. A. Hassani Gangaraj, M. G. Silveirinha, and G. W. Hanson, "Berry phase, Berry potential, and Chern number for continuum bianisotropic material from a classical electromagnetics perspective," IEEE J. Multiscale Multiphys. Comput. Tech. 2, 3–17 (2017).
- ⁵L. Lu, J. D. Joannopoulos, and M. Soljačić, "Topological photonics," Nat. Photonics 8, 821–829 (2014).
- ⁶M. C. Rechtsman, J. M. Zeuner, Y. Plotnik, Y. Lumer, D. Podolsky, F. Dreisow, S. Nolte, M. Segev, and A. Szameit, "Photonic Floquet topological insulators," Nature **496**, 196 (2013).
- ⁷F. D. M. Haldane and S. Raghu, "Possible realization of directional optical waveguides in photonic crystals with broken time-reversal symmetry," Phys. Rev. Lett. 100, 013904 (2008).
- ⁸S. Pakniyat, A. M. Holmes, G. W. Hanson, S. A. H. Gangaraj, M. Antezza, M. G. Silveirinha, S. Jam, and F. Monticone, "Non-reciprocal, robust surface plasmon polaritons on gyrotropic interfaces," IEEE Trans. Antennas Propag. 68, 3718–3729 (2020).

- ⁹M. G. Silveirinha, S. A. H. Gangaraj, G. W. Hanson, and M. Antezza, "Fluctuation-induced forces on an atom near a photonic topological material," Phys. Rev. A **97**, 022509 (2018).
- 10É. Moncada-Villa, V. Fernández-Hurtado, F. J. García-Vidal, A. García-Martín, and J. C. Cuevas, "Magnetic field control of near-field radiative heat transfer and the realization of highly tunable hyperbolic thermal emitters," Phys. Rev. B 92, 125418 (2015).
- ¹¹F. Fan, S. T. Xu, X. H. Wang, and S. J. Chang, "Terahertz polarization converter and one-way transmission based on double-layer magneto-plasmonics of magnetized InSb," Opt. Express 24, 26431–26443 (2016).
- ¹²K. L. Tsakmakidis, L. Shen, S. A. Schulz, X. Zheng, J. Upham, X. Deng, H. Altug, A. F. Vakakis, and R. W. Boyd, "Breaking Lorentz reciprocity to overcome the time-bandwidth limit in physics and engineering," Science 356, 1260–1264 (2017).
- ¹³S. A. H. Gangaraj and F. Monticone, "Topologically-protected one-way leaky waves in nonreciprocal plasmonic structures," J. Phys.: Condens. Matter 30, 104002 (2018).
- ¹⁴E. Moncada-Villa, A. I. Fernández-Domínguez, and J. C. Cuevas, "Magnetic-field controlled anomalous refraction in doped semiconductors," J. Opt. Soc. Am. B 36, 935–941 (2019).
- ¹⁵H. Hu, L. Liu, X. Hu, D. Liu, and D. Gao, "Routing emission with a multi-channel nonreciprocal waveguide," Photon. Res. 7, 642–646 (2019).
- ¹⁶W. Zhang and X. Zhang, "Backscattering-immune computing of spatial differentiation by nonreciprocal plasmonics," Phys. Rev. Appl. 11, 054033 (2019).
- 17S. A. H. Gangaraj, B. Jin, C. Argyropoulos, and F. Monticone, "Broadband field enhancement and giant nonlinear effects in terminated unidirectional plasmonic waveguides," arXiv:2006.13393 (2020).
- ¹⁸E. D. Palik, R. Kaplan, R. W. Gammon, H. Kaplan, R. F. Wallis, and J. J. Quinn, "Coupled surface magnetoplasmon-optic-phonon polariton modes on InSb," Phys. Rev. B **13**, 2497–2506 (1976).
- ¹⁹E. D. Palik and J. K. Furdyna, "Infrared and microwave magnetoplasma effects in semiconductors," Rep. Prog. Phys. 33, 1193 (1970).
- ²⁰G. W. Hanson, S. Ali Hassani Gangaraj, and A. Nemilentsau, "Notes on photonic topological insulators and scattering-protected edge states—A brief introduction," arXiv:1602.02425 (2016).
- ²¹S. Buddhiraju, Y. Shi, A. Song, C. Wojcik, M. Minkov, I. Williamson, A. Dutt, and S. Fan, "Absence of unidirectionally propagating surface plasmon-polaritons in nonreciprocal plasmonics," Nat. Commun. 11, 674 (2020).
- ²²S. Ali Hassani Gangaraj and F. Monticone, "Do truly unidirectional surface plasmon-polaritons exist?," Optica 6, 1158–1165 (2019).
- ²³M. S. Kushwaha, "Plasmons and magnetoplasmons in semiconductor heterostructures," Surf. Sci. Rep. 1, 1–416 (2001).
- ²⁴MTI Corp., see https://www.mtixtl.com for InSb crystals specification.
- 25S. Pandey, B. Gupta, A. Chanana, and A. Nahata, "Non-Drude like behaviour of metals in the terahertz spectral range," Adv. Phys.: X 1, 176 (2016).
- 26Y. Liang, S. Pakniyat, Y. Xiang, F. Shi, G. W. Hanson, and C. Cen, "Tunable THz reflections induced by gapped magneto-plasmons in InSb," Opt. Mater. (submitted) (2020).